

When a real-life quantity increases or decreases by a fixed percent each year (or other time period), the amount y of the quantity after t years can be modeled by one of the following equations:

Exponential Growth Model	Exponential Decay Model
$y = a(1+r)^t$	$y = a(1-r)^t$

In these equations, $a =$ initial amount

$r =$ percentage rate

$1 + r =$ growth factor

$1 - r =$ decay factor

(b) ex: growing by 11%
 $r = .11$
 $1+r = 1.11$

Example 2

a.) In 1970, the population of Kern County, California, where Bakersfield is located, was about 333,000. From 1970 to 2000, the county population grew at an average annual rate of about 2.4%.

i.) Write an exponential model giving the population P of Kern County t years after 1970.

$$P = 333,000(1 + 0.024)^t$$

ii.) About how many people lived in Kern County in 1990? *1990-1970=20

$$P = 333,000(1.024)^{20} = \underline{535,110 \text{ people}}$$

b.) A new car costs \$25,000. The value of the car decreases by 15% each year.

i.) Write an exponential model giving the car's value y (in dollars) after t years.

$$y = 25,000(1 - .15)^t$$

ii.) Graph your equation from part i and use the graph to estimate the value of the car after 4 years.

$$y = 25,000(.85)^4 = \underline{\$13,050.16}$$

Compound Interest interest that is paid on the initial investment and on previously earned interest

$$A = P\left(1 + \frac{r}{n}\right)^{nt}$$

$P =$ principal

$r =$ annual rate

$n =$ times per year

$t =$ time

$A =$ amount in account

Example 3

You deposit \$5500 in an account that pays 3.6% annual interest. Find the balance after 2 years if interest is compounded with the given frequency.

a.) semiannually

$$A = 5500 \left(1 + \frac{0.036}{2}\right)^{2t}$$

$$A = 5500 \left(1 + \frac{0.036}{2}\right)^{2 \cdot 2}$$

$$A = \$5906.82$$

b.) monthly

$$A = 5500 \left(1 + \frac{0.036}{12}\right)^{12t}$$

$$A = 5500 \left(1 + \frac{0.036}{12}\right)^{24}$$

$$A = \$5909.97$$

Section 3 – Use Functions Involving e

n	10^1	10^2	10^3	10^4	10^5	10^6
$\left(1 + \frac{1}{n}\right)^n$						

As n gets bigger and bigger (approaches ∞), $\left(1 + \frac{1}{n}\right)^n$ approaches _____. This number is called _____ or _____ and is denoted _____.

Example 1

Simplify the expression.

a.) $e^9 \cdot e^6$

b.) $\frac{60e^8}{12e^3}$

c.) $(-10e^{-5x})^3$

Example 2

Use a calculator to evaluate the expression.

a.) e^6

b.) $e^{-0.28}$

c.) $e^{3/4}$