

7.7 Homework

Name: Key(1-3) Write an exponential function $y = ab^x$ whose graph passes through the given points.

1) (1,3), (2,12)

$$y = \frac{3}{4} \cdot 4^x$$

2) (3,27), (5,243)

$$y = 3^x$$

3) (2,6.4), (5,409.6)

$$y = 0.4 \cdot 4^x$$

4) A doctor measures an astronaut's pulse rate y (in beats per minute) at various times x (in minutes) after the astronaut has finished exercising. The astronaut's resting pulse rate is 70 beats per minute. Write an exponential model for the data, given the following information:

At 2 minutes, the pulse rate was 132 bpm

At 10 minutes, the pulse rate was 78 bpm

$$\begin{aligned}
 132 &= a \cdot b^2 \\
 a &= \frac{132}{b^2}
 \end{aligned}
 \left\{
 \begin{aligned}
 78 &= a \cdot b^{10} \\
 78 &= \left(\frac{132}{b^2}\right) b^{10} \\
 78 &= 132 \cdot b^8 \\
 \frac{78}{132} &= b^8 \\
 b &= \sqrt[8]{\frac{78}{132}}
 \end{aligned}
 \right.$$

$$\left\{
 \begin{aligned}
 132 &= a \cdot \left(\sqrt[8]{\frac{78}{132}}\right)^2 \\
 a &= 150.56 \\
 b &= 0.94
 \end{aligned}
 \right.$$

$$\boxed{y = 150.56(0.94)^x}$$